

# Exercise 8.5

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This algorithm can work by running two instances of the regular frequent-items problem in parallel.

More specifically, we run two instances, each of which reset after scanning over  $2W$  items, where one instance resets starting at 0 items and the other starting at  $W$  items. Furthermore, each of these instances determines the set of  $\frac{\epsilon}{2}$ -frequent items. Then, whenever an answer needs to be provided at a given point, the current set of  $\frac{\epsilon}{2}$ -frequent items maintained by the longest-running instance will be returned.

The reason this works is that, at any point in time, any item which is  $\epsilon$ -frequent over the last  $W$  items will also be  $\frac{\epsilon}{2}$ -frequent among the last  $2W$  items. Since there is an instance which has run over at least the past  $W$  items (*but not more than  $2W$  items*), there will always be one instance which has a set of at most  $\frac{2}{\epsilon}$  items which are  $\frac{\epsilon}{2}$ -frequent among the last (at most)  $2W$  items; all  $\epsilon$ -frequent items over the last  $W$  items must be included in this set.